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Authors

Dekel, Eddie Farrell, Joseph

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UNIVERSITY OF CALIFORNIA AT BERKELEY

Department of Economics

Berkeley, California 94720

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One-Sided Patience with One-Sided Communication Does Not Justify Stackelberg Equilibrium

Eddie Dekel and Joseph Farrell University of California, Berkeley

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Key words: Communication, renegotiation, repeated games, Stackelberg equilibrium

Abstract

The theory of games (with complete information) in which a single patient long-run player faces a succession of short-run opponents cannot plausibly be used to justify the Stackelberg solution concept, because if that player can select which subgame-perfect equilibrium is to be played then she can presumably also change her selection. Consequently, while she can choose among one-shot Nash outcomes, she cannot achieve the Stackelberg outcome.

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One-Sided Patience With One-Sided Communication Does Not Justify Stackelberg Equilibrium

Eddie Dekel and Joseph Farrell

The Stackelberg equilibrium concept has two possible justifications. The first applies to a one-shot game in which one player moves first (and the other observes the former's move before choosing his own). But many applications do not fit this case: instead, the game is infinitely repeated and the Stackelberg equilibrium in the stage-game is felt to be justified because one (and only one) player can somehow "commit" over time to a particular stage-game action. In particular, it may seem intuitively appealing that if one player is long-lived and has a discount factor close to 1, while her opponent has a very low discount factor (or is represented by a sequence of short-run players), then the former will be able to take the role of Stackelberg leader, and in each period the one-shot Stackelberg outcome, s, will occur.

There are several possible arguments by which one might hope to formalize this intuition. First, Fudenberg and Levine (1989) show that if there is incomplete information of a certain kind about the long-run player's payoffs, then she will achieve an overall payoff close to that from s being played each period. More precisely, say that the long-run player is a "Stackelberg type" if it is a strictly dominant strategy for her to play her Stackelberg action s_L in each period. Fudenberg and Levine show that if the short-run players assign strictly positive probability to the long-run player being a Stackelberg type, then in any Nash equilibrium the long-run player will achieve a payoff close to that from s being played each period. The result follows from a "reputation effects" argument (Kreps, Milgrom, Roberts and Wilson, 1982; Fudenberg and Maskin, 1986): the long-run player will mimic the Stackelberg type. But, for this justification, we must assume that the short-run players believe that with positive probability the long-run player is a Stackelberg type. Although it is often plausible that there is incomplete information about the precise payoffs, there are surely many situations in which it is common knowledge that the long-run player is not the Stackelberg type.

In this note, we examine another method, which rests on the claim that even with complete information, the long-run player can credibly commit to any form of behavior, and will therefore choose to commit to the most profitable form of behavior, i.e., playing s_L always. More precisely:

A related approach (Dekel, Fudenberg and Levine, in progress) is to show that the only stable equilibrium in the repeated game is the repeated Stackelberg equilibrium. This approach, however, relies on a very strong refinement of Nash equilibrium and hence might not be totally compelling.

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(i) there is a subgame-perfect equilibrium in which the long-run player always plays s_L ; moreover, (ii) this yields her best payoff among subgame-perfect equilibria. Intuitively, one might therefore think that (iii) if she controls the communication she will select this equilibrium. Parts (i) and (ii) of this claim have been justified by Fudenberg, Kreps and Maskin (1988), as we discuss below. Part (iii), however, is invalid, as we will show.

Fudenberg, Kreps, and Maskin characterized the subgame-perfect equilibria of games in which one player, who has a discount factor δ close to 1, plays against a succession of "short-run" players, each of whom plays the game only once (although he observes the entire history).² They derive a "Folk Theorem" result as follows. Restrict attention to action-pairs in which the short-run player plays a best response to the long-run player's move. Defining feasibility and minimax payoffs relative to this restricted set of action-pairs, they show that, as $\delta \to 1$, all feasible, strictly individually rational, outcomes become subgame-perfect equilibria. In particular, if the long-run player's mixed strategies are observable, then there exists a subgame perfect equilibrium in which along the equilibrium path s is played in each period.³ Abusing terminology, we call this subgame-perfect equilibrium "the Stackelberg equilibrium". Fudenberg, Kreps and Maskin also show that there is no subgame-perfect equilibrium that gives the long-run player a greater payoff than she gets in this equilibrium.

To conclude from this that the Stackelberg equilibrium may be expected in such a game, we must also assume that the long-run player can choose which subgame-perfect equilibrium will be played. Intuitively, this may seem reasonable: after all, she has in some sense the most at stake, and might well be expected to control the channels of communication. In any case, whether plausible or not, the assumption is necessary in order to justify Stackelberg equilibrium in this fashion.

But if the long-run player can select an equilibrium at the beginning of the game, it is natural to suppose that she can also re-select later. This observation suggests an analogy to the theory of renegotiation-proof equilibrium. There, it is supposed that players jointly negotiate an equilibrium of the repeated game, but cannot commit themselves not to renegotiate later, if doing so would yield a strictly better continuation outcome for all of them. Here, we suppose that one player

² In fact, they allowed for more than one long-run player and for more than one short-run player, but we restrict our attention to the simplest case.

³ The reader is referred to their paper for a discussion of the subtle issues that arise if mixed strategies are not observable.

⁴ Bernheim and Ray (1989) and Farrell and Maskin (1989) independently developed the theory reviewed below. See Pearce (1988) for a different approach to renegotiation, and Benoit and Krishna (1988) for the finitely-repeated case.

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can unilaterally select an equilibrium at the beginning; unless the opportunities for communication occur only once, we must also suppose that she can re-select later, if doing so would yield a strictly better continuation outcome for her.

Farrell and Maskin (1989) call a subgame-perfect equilibrium "weakly renegotiation-proof equilibrium" if no two of its continuation equilibria are strictly Pareto-ranked. In the same spirit, we call a subgame-perfect equilibrium "weakly re-selection-proof" if no two of its continuation equilibria are strictly ranked according to the long-run player's payoffs. Like weak renegotiation-proofness, this seems necessary for credibility: indeed, the assumption that a player who controls communication can achieve her best equilibrium seems even more compelling than the assumption that players jointly can always agree on, and thereby achieve, Pareto improvements.

But, unless it happens also to be a one-shot Nash equilibrium, the Stackelberg equilibrium is not weakly re-selection-proof. To see this, note that in any weakly re-selection-proof equilibrium, every two continuation equilibria must yield the same continuation payoff to the long-run player. Therefore she cannot be threatened by future consequences of her current opportunism, and so she will always choose short-run best responses. Consequently, any weakly re-selection-proof equilibrium must specify, in every period, a one-shot Nash equilibrium of the stage-game.

We conclude that the Fudenberg-Kreps-Maskin theory of games with one patient (long-run) player facing one or more short-run player(s) cannot justify the Stackelberg equilibrium concept, absent some explanation of why the long-run player has selection power but not re-selection power.

Because weak re-selection-proofness is a necessary condition, we can rule out subgame-perfect equilibria, such as the Stackelberg equilibrium, that fail to satisfy it. But it is by no means a sufficient condition: for example, suppose that the stage-game has two Nash equilibria, e_1 and e_2 , yielding the long-run player payoffs 1 and 2 respectively. Then "always play e_1 , regardless of history" is a weakly re-selection-proof equilibrium (it has no continuation equilibria other than itself); but it is plainly implausible.

This leads us to define a "strongly re-selection-proof" equilibrium (by analogy with strongly renegotiation-proof equilibrium) as a weakly re-selection-proof equilibrium no continuation equilibrium of which is strictly dominated, for the long-run player, by any weakly re-selection-proof equilibrium. Like strongly renegotiation-proof equilibrium, strongly re-selection-proof equilibrium seems convincing if it exists.

But it is evident that strongly re-selection-proof equilibrium always exists, and that such equilibria are precisely the weakly re-selection-proof equilibria in which each period's one-shot Nash

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equilibrium gives the long-run player her maximum one-shot Nash equilibrium payoff.⁵ This for-malizes the idea that the long-run player can choose among one-shot Nash equilibria, although (because she cannot commit not to re-select) she can do no better than that.

⁵ For a typical stage-game, of course, there is just one such one-shot Nash equilibrium, so there is a unique strongly re-selection-proof equilibrium.

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