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The Constrained Asset Share Estimation (CASE)
Method: Testing Mean-Variance Efficiency
of the U.S. Stock Market \*

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Key words: CAPM, stock market, portfolio-balance, mean variance efficiency

#### <u>Abstract</u>

We apply the method of constrained asset share estimation (CASE) to test the mean-variance efficiency (MVE) of the stock market. This method allows conditional expected returns to vary in unrestricted ways, given investor preferences. We also allow conditional variances to follow an ARCH process. The data estimate reasonably the price of risk, though they are unable to reject risk neutrality. We reject the restrictions implied by MVE, although changing conditional variances improve statistically upon measured market efficiency. We find that unrestricted asset-share and ARCH models held forecast excess returns. Once MVE is imposed, however, this forecasting ability disappears.

JEL Classification: 313

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, The Constrained Asset Share Estimation (CASE) Method: Testing Mean-Variance Efficiency of the U.S. Stock Market

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This paper uses a technique that we call Constrained Asset Share Estimation (CASE) to test the conditional mean-variance efficiency (MVE) of the U.S. stock market. The technique is useful in time-series tests of simple asset pricing models because it allows estimated expected returns to vary in an unrestricted way. It was first applied in a macroeconomic context in which the "market" portfolio included not only equities, but also money, bonds and real estate. It has since been applied more widely to other portfolios and has been extended to allow for variation in conditional second as well as first moments, as in an autoregressive-conditional-heteroskedasticity (ARCH) model.<sup>2</sup>

There is still a need for a clear statement of the advantages of the CASE method over earlier tests of the MVE hypothesis for the stock market. Briefly, these advantages are of two sorts. First, the technique does not impose the condition that expected returns are constant over time, or even that they change in a slowly moving way. Rather it allows expected returns to vary freely, as they must, for example, whenever new information which may not be observed by the econometrician becomes available to the investor. In addition, in some of the tests below we allow second moments

<sup>&</sup>lt;sup>1</sup>See Frankel (1982, 1985a), Frankel and Dickens (1984), Frankel and Engel (1984), and Wills (1982).

<sup>&</sup>lt;sup>2</sup>Ferson, Kandel and Stambaugh (1987) and Rayner (1986) test the constant-variance version on stock portfolios. Bodurtha and Mark (1988), Bollerslev, Engle and Wooldridge (1987) and Engel and Rodrigues (1989), test a version which allows for changing conditional second moments on portfolios, respectively, of stocks, domestic bonds, and short-term bills denominated in different currencies.

<sup>&</sup>lt;sup>3</sup> In the tests below, expected excess returns are allowed to vary in a completely general way as functions of the asset shares, requiring only that a set of preference parameters consistent with the Hara class of utility functions remain constant.

to vary according to an ARCH process.<sup>4</sup> Allowing for such variation in conditional moments is essential for a properly specified test of MVE. In fact, there is considerable evidence that both the conditional expectation and conditional variance of excess returns contain important predictable components.<sup>5</sup> Beyond being a more realistic specification, allowing the CAPM betas to evolve over time has the additional advantage that longer time series can be used to test MVE. In the past, tests of MVE coped with changing moments by using short test periods, usually 5 years or less.<sup>6</sup>

The second, and perhaps most important, advantage implicit in the CASE method is that it nests MVE in a more general, but economically meaningful, theory of portfolio determination. In contrast, most tests of the null hypothesis of MVE have no clear alternative hypothesis. This feature is particularly important because many tests do in fact reject MVE; when one rejects the null hypothesis it is crucial to have some idea of what the alternative is. In the central tests below, the alternative to MVE is that investors' portfolio shares are linearly related to expected returns, but that investors do not compute covariances with the market portfolio in the precise way that MVE would imply they should. The alternative hypothesis is the more general portfolio-balance approach to asset demands that was first introduced by Tobin (1958, 1969). The problem he was addressing was the relationship between expected returns and the demand for bonds and other assets. Even though CAPM originally grew out of the portfolio-balance model, as an attempt by Tobin (1958) and Markowitz (1952) to bring more structure to bear on the problem, most modern testing of CAPM has departed from this original context.

<sup>&</sup>lt;sup>4</sup>The ARCH process does not allow second moments to vary freely however. It is analogous to estimating the first moments by an ARIMA process, in which this period's expectation is related to recent realisations, rather than by the CASE technique, in which expectations can vary freely.

<sup>&</sup>lt;sup>5</sup>See, for example, Fama and French (1988) and Poterba and Summers (1987) for evidence on the predictability of stock market returns, and Bollerslev (1985) and Bollerslev, Engle and Wooldridge (1988) for evidence on the predictability of conditional variances of excess returns. These findings coupled with the results of Hansen and Richard (1987), who show that the conditionally and unconditionally mean-variance efficient frontiers are generally different, suggest that such variation in conditional moments is important for tests of MVE.

<sup>&</sup>lt;sup>6</sup>There are two problems with this procedure. First, there appears to be a substantial amount of conditional variation in both first and second moments over forecast horisons of much less than 5 years (see for example Fama and French, 1988, Pindyck, 1984, and Poterba and Summers, 1986). Second, while limiting time-series samples to 5 years makes the assumption of constant conditional moments more believable, it also reduces the power of tests of MVE. Low power can potentially explain the lack of any measured relationship between risk and return in tests of MVE (see Schwert, 1983, Gibbons, Ross and Shanken, 1986, MacKinlay, 1987, and Gibbons and Shanken, 1987). The use of longer time series also reduces the need to develop small-sample test statistics, such as that suggested by Shanken (1987). With large time-series samples, the distributions of conventional test statistics are likely to be closer to their asymptotic approximations.

<sup>&</sup>lt;sup>7</sup>One possibility is that the managers of pension funds and the other funds that hold most equities are concerned only with minimizing the variance of their own performance, rather than computing covariances with the aggregate portfolios held by individuals as they in theory should.

Tobin (1983) confirms that his original work "was intended primarily as a contribution to positive macroeconomics rather than to management science" (p. 236). In other words, the motivation was to be able to examine questions like the following: When the government increases the stock of debt by \$1 billion, by how much must the interest rate rise for investors to hold the additional debt willingly? The framework of mean-variance optimisation was a tool to be used in this problem.

Our tests below emphasize the nested nature of the hypotheses we consider. We pay special attention to the importance of ARCH vs. MVE vs. the asset shares themselves in explaining risk premia. The broad findings can be summarized as follows. First, we find that stock-market shares by themselves have statistically significant explanatory power in predicting monthly excess stock returns. This is what we would expect if the stock market is mean-variance efficient and if required returns change over time. However, we reject the restrictions implied by constant-variance MVE. Moreover, the ability of asset shares to forecast future excess returns disappears once the MVE restrictions are imposed. Something very different than MVE appears to be responsible for asset shares' ability to predict stock returns.

One might conjecture that MVE holds and that these results are an artifact of the maintained assumption that conditional variances are constant. Indeed, we find that the data reject the hypothesis that the market is mean-variance efficient with a constant variance against the alternative that the market is mean-variance efficient with a conditional covariance matrix that evolves according to an ARCH process. Time-varying second moments therefore move the mean-variance efficient frontier closer to the market portfolio. This is good news for ARCH, but not for MVE: we cannot reject the hypothesis that the ARCH-MVE model can explain no portion of excess returns. Nevertheless, the data produce an estimate, 2.0, for the price of risk, which is a sensible estimate under its interpretation as the coefficient of relative risk aversion. The standard error is about 1.5. Thus, while we cannot reject the hypothesis that investors are risk neutral, we can reject hypotheses that they are strongly risk loving or risk averse.

Finally, we test a generalized ARCH specification, which does not impose MVE, against the null hypothesis that the market is conditionally mean-variance efficient and that conditional variances evolve according to an ARCH process. Once again we reject the restrictions imposed by by conditional MVE.

The paper is structured as follows. Sections 1 and 2 briefly describe the model and the data, respectively. Section 3 tests for constant-variance MVE. We introduce our ARCH specification in section 4, and test an unrestricted model as well as an ARCH-MVE system. Section 5 summarizes our general nesting procedure for the hypotheses of interest and offers our conclusions.

#### 1. The model

Mean-variance efficiency implies that the vector of conditional risk premia is a linear combination of the asset shares in the portfolio, with the weights proportional to the conditional variance of asset returns:

$$E_t(r_{t+1}) = \rho_t \Omega_t \lambda_t, \tag{1}$$

where  $E_t(r_{t+1})$  is the expected excess return above the riskless rate on an  $N \times 1$  vector of assets conditional on all information available at time t,  $\Omega_t$  is the conditional variance of returns between t and t+1,  $\lambda_t$  is the  $N \times 1$  vector of portfolio weights, with  $\sum_{i=1}^{N} \lambda_{t,i} = 1$ , and  $\rho_t$  is the price of risk. If the aggregate stock portfolio is the "market" portfolio, MVE is equivalent to the CAPM, and the parameter  $\rho$  is to be interpreted as the coefficient of relative risk aversion. Note that the right-hand side of (1) is equivalent to the risk-adjusted conditional expected return on the aggregate (or market) portfolio,

$$E_t(r_{t+1}) = \beta_t E_t(m_{t+1}) = \beta_t \lambda_t' E_t(r_{t+1}),$$

where

$$\beta_t = \frac{\Omega_t \lambda_t}{\lambda_t' \Omega_t \lambda_t} = \frac{\operatorname{cov}(m_{t+1}, r_{t+1})}{\operatorname{var}(m_{t+1})}.$$

This expression makes it clear that the vector of sub-portfolio  $\beta_t$ s varies both with the shares of assets in the portfolio,  $\lambda_t$ , and the conditional covariance matrix,  $\Omega_t$ , and thus may move substantially over short time intervals. Also, note that given preferences and  $\Omega_t$ , (1) is a complete model of expected excess returns: MVE implies that asset shares are sufficient statistics for optimal forecasts of excess returns.

Under rational expectations, we can replace the vector of expected excess returns with the actual returns by including a prediction error that is orthogonal to all information at time t:

$$r_{t+1} = \rho_t \Omega_t \lambda_t + \epsilon_{t+1}, \tag{2}$$

where  $\epsilon_{t+1} = r_{t+1} - E_t(r_{t+1})$ . The insight in Frankel (1982) was that information about the conditional covariance matrix of returns can be obtained from the error terms, since under MVE:

$$\Omega_t = E_t(\epsilon_{t+1}\epsilon'_{t+1}). \tag{3}$$

<sup>&</sup>lt;sup>9</sup>As is well-known, MVE can be derived from more general intertemporal optimization only under special circumstances, not likely to include a time-varying covariance matrix. But there is much interest in testing MVE nonetheless, both with and without time-varying covariances.

MVE therefore imposes a set of restrictions that are highly nonlinear in that they constitute proportionality between the coefficient matrix and the variance-covariance matrix of the error term in (2).

To evaluate (3), we must take a position on whether  $\Omega_t$  is constant over time. In sections 3 and 4 below, we assume that  $\Omega_t$  is constant and that it follows an ARCH process, respectively. We test the hypotheses that MVE holds against more general alternatives in which investors forecast excess returns as a function of asset shares and past prediction errors. The exact specifications for the alternative hypotheses are discussed in sections 3 and 4. We also test the MVE hypotheses above, as well as the more general alternatives, against an even more restrictive null hypothesis: that investors expect conditional excess returns to be zero. The results of these tests are also discussed in sections 3 and 4. Section 5 presents a diagram which makes it easy to see the results of our nested hypothesis tests.

#### 2. The data

Our tests use monthly stock returns from the New York and American Stock Exchanges from January 1955 to December 1984. Because of the computational difficulties in estimating (2) we were forced to reduce the size of the cross section. In the tests below we aggregate stocks into N = 11 (and sometimes 7) industry portfolios.

Table 1 describes the aggregation of stocks into industry portfolios. The returns for each portfolio are value-weighted average returns. The  $N \times 1$  vector of portfolio shares,  $\lambda_i$ , is the value of the stocks in the portfolios as a fraction of the total value of all stocks. Because it is desirable to group together equities that have highly correlated returns, we tried to put similar industries into the same portfolio. Stambaugh (1982) aggregates into 20 industries, roughly by type of final output. We further aggregate into 11 industries, combining some of Stambaugh's catagories. Table 1 shows Stambaugh's 20 industries, as well as the 11-industry aggregation that we use to perform our maximum likelihood tests of MVE. Table 1 also reports a 7-industry aggregation that we use for the ARCH estimation in section 4.

 $<sup>^{10}</sup>$  If there are N assets, the computation involves a parameter matrix of dimension  $N(N-1)/2 \times N(N-1)/2$  that must be repeatedly inverted. Engel and Rodrigues (1988) offer a Wald test version of the CASE test that gets around this problem, and allows one to consider larger vectors of assets. We apply it in Section 3 below.

<sup>13</sup> On the other hand, we would not want to include together the suppliers of intermediate products and the producers of final output in the same industry. When steel prices rise, the cost of producing autos increases so that it is possible that steel producers' profits rise when auto manufacturers profits decline.

The value shares,  $\lambda_t$ , are used to predict excess returns between time t and t+1. The shares are measured monthly from the last day of January 1955 to the last day of November 1984 (359 observations), while the returns are calculated as the dividend plus appreciation over the previous month beginning the last day of February 1955 and ending the last day of December 1984. All returns are nominal excess returns above the return on one-month Treasury bills recorded by Ibbotson Associates (1986).

#### 3. Tests of MVE with constant conditional variances.

If relative risk aversion and the return covariance matrix are constant,  $\rho_t \Omega_t = \rho \Omega$ , we can write demands for assets as a function of their own rate of return and returns on all other equities. The portfolio-balance model of Tobin (1958, 1969), representing a general relationship between asset demands and expected returns, can be written as:

$$\lambda_t = \mathbf{B}E_t(r_{t+1}),\tag{4}$$

where B is an  $N \times N$  matrix of coefficients. By inverting the system of equations in (4), we obtain an expression for expected excess returns,

$$E_t(r_{t+1}) = \mathbf{A}\lambda_t, \tag{5}$$

where  $A = B^{-1}$ . This system of equations representing the portfolio-balance model, is a generalization of MVE. MVE imposes the restriction that the matrix of coefficients A be proportional to the variance of the forecast error,  $\epsilon_{t+1}$ .

Hence an insight of the CASE method: MVE can be viewed as the null hypothesis in a test where the alternative hypothesis is the more general unconstrained portfolio balance model. Using ex post returns, (5) can be written:

$$\mathbf{r}_{t+1} = \mathbf{A}\lambda_t + \epsilon_{t+1}. \tag{6}$$

Although the values of the equities are endogenous variables in an economic sense, they are still uncorrelated with the prediction errors, which under rational expectations are uncorrelated with all information available at time t. Thus the system in (6) can be estimated consistently using ordinary least squares, equation by equation.<sup>12</sup>

<sup>&</sup>lt;sup>12</sup>Note that the N asset shares,  $\lambda_{t,1} \dots \lambda_{t,N}$ , are perfectly collinear because they sum to 1. This does not pose a problem for the estimation of (7), however, because the equations do not include a constant term.

#### 3.1. A likelihood-ratio test of MVE

Table 2 reports the results from estimating the unconstrained system of equations (6). Few of the coefficients individually are significantly different from zero. Unsurprisingly, the  $R^2$ s are not very high, and none exceeds .10. We can reject at the 95 percent level the hypothesis that the asset shares have no explanatory power for excess stock returns. The log-likelihood value for the 11 equation system is 8709.35. The log-likelihood when all 121 coefficient are constrained to be zero is 8592.57. Twice the difference is distributed as  $\chi^2_{121}$ . The value of the statistic is 233.56 compared with a critical value of 147.39.<sup>1314</sup>

There is mixed support for one of our assumptions – that forecasts are rational. This assumption implies that there is no serial correlation in forecast errors. We performed Breusch-Godfrey tests for serial correlation from orders 1 to 20. We report the chi-square statistics only for the tests of the existence of 20th order autoregressive or moving average errors. In only four of the regressions can we reject the null hypothesis of no serial correlation up to 20th order at the 95 percent level.<sup>15</sup>

Under the MVE hypothesis, this unconstrained system of inverted asset demand equations is not estimated efficiently. If we impose more structure on the system we can hope to improve the precision of our parameter estimates. So we will estimate the system of equations in (6) imposing the MVE constraints:

$$r_{t+1} = \rho \Omega \lambda_t + \epsilon_{t+1}, \tag{7}$$

so that  $A = \rho\Omega$ . The N equation system (7) must be estimated by maximum likelihood techniques, imposing an unusual cross-equation restriction – between the matrix of coefficients in the regressions and the variance matrix of the regression errors. Note that the assumption that  $\Omega$  is constant is not the same as the usual assumption in MVE tests of constant betas and expected returns. As we saw in the previous section, even with a constant covariance matrix, the betas, and hence the expected returns on all securities including the aggregate or "market" portfolio, will vary over time

<sup>&</sup>lt;sup>18</sup>The 99 percent critical value is 159.32.

<sup>&</sup>lt;sup>14</sup>The only prior belief we have about the coefficients is that the return on asset j is likely to be positively related to the share of asset j in the total portfolio. If we think of the market portfolio as comprised only of stocks, then in equilibrium investors will demand a higher return from a given stock portfolio the more of it they are required to hold. Table 2 shows that in 8 out of the 11 regressions this own-coefficient is negative (and significantly negative for industries 2 and 7). It is not significantly positive in any of the regressions.

<sup>&</sup>lt;sup>15</sup> Similar tests for serial correlation which allow for heteroskedasticity were performed. The results were not importantly different from those reported above.

in a general, unrestricted way.<sup>16</sup> Table 3 reports the maximum likelihood results of (7). The log-likelihood value is necessarily lower than the log-likelihood for (6) because (7) is a restricted form of (7): 8593.68 (as compared to the unrestricted log-likelihood of 8709.35).

Is the difference statistically significant? We report a chi-square statistic for the restrictions implied by (8). This is the CASE test of the MVE hypothesis against the more general portfoliobalance model. We impose 120 restrictions on the unconstrained system (121 coefficients are constrained to be proportional to their corresponding elements in the variance matrix). The test statistic is distributed  $\chi^2_{120}$ , and its value is 231.34. The answer is that we easily reject the hypothesis of MVE at the 99 percent level.<sup>17</sup>

If one were willing to accept the MVE estimates on the basis of prior beliefs, they yield in some ways much more plausible asset pricing equations. We noted that in the unconstrained regressions we frequently found that an increase in an asset share would actually decrease that asset's expected return. That is not possible with the constrained MVE estimates. Also, the point estimate of  $\rho$ , which can be interpreted as the coefficient of relative risk aversion under the assumption that the  $\lambda_t$  are shares of the complete market portfolio, is very plausible – 2.03. It is very close to the "Samuelson presumption" of a likely value for average risk aversion. The coefficient is not estimated precisely, however, as it is not statistically different from zero at the 95 percent level. But its 95 percent confidence interval ranges only up to about 5.3 – still a believable estimate for average risk aversion.

On the other hand, the constrained model does a very poor job of predicting excess returns. The failure to reject the hypothesis that  $\rho = 0$  implies that asset shares provide no statistically significant explanatory power for risk premia under the MVE restrictions, because the coefficients on the shares are all multiples of  $\rho$ .<sup>18</sup> In other words, MVE vitiates the predictive power of the asset shares alone.

The estimates reported in Tables 2 and 3 calculate the shares as a fraction of total equity investment. If, however, there are positive net holdings of the riskless asset, then the shares should properly be calculated as a fraction of total equity investment plus the total net value of the riskless

<sup>16</sup> Frankel (1985a)

<sup>17</sup> Comparing the results from table 3 to table 2, it is easy to see the source of the rejection. When the coefficients are constrained, they are much smaller than when they are unconstrained. Under the MVE constraints, an increase in the share of an asset has a much smaller impact on risk premia.

<sup>18</sup> Under the MVE restrictions, constraining \$\rho\$ to be zero lowers the log-likelihood value by 1.1.

asset. The riskless asset could have a positive net value if the government issues riskless short-term bonds, and investors consider government bonds to be additions to net wealth (so that they do not fully discount future tax liabilities) or if the government issues money. We estimated the model under the assumption that the relevant measure of the net supply is the value of all government bonds (which are calculated by Cox, 1985), and again under the assumption that the value of outstanding Treasury bills measure the net supply of the riskless asset. In both cases, there was almost no change in the estimates.

We considered two other formulations which apply when  $\rho$  is interpreted as the coefficient of relative risk aversion, besides assuming that it is constant. In the first, we assumed constant absolute risk aversion. In that case,  $\rho_t = bW_t$  where b is the coefficient of absolute risk aversion and  $W_t$  is the value of all equities at time t. In the second, we considered a more general formulation consistent with the Hara class of utility functions,  $\rho_t = a + bW_t$ . If b = 0 we have the constant relative risk aversion case, and if a = 0 we have constant absolute risk aversion. Again, however, these versions of the model failed to improve the constrained model's performance.<sup>19</sup>

#### 3.2. A Wald test of MVE

Maximum likelihood estimation of MVE is a difficult task. The constraints between the coefficients and the variance cause grave problems in finding the maximum of the likelihood function. The estimation is expensive and time consuming. The entire system must be estimated simultaneously, which in the case of the 11-asset system means simultaneously estimating 122 coefficients. The complexity of the problem increases with the square of the number of equations and assets. If we were to estimate the model even for all 20 of Stambaugh's original portfolios, it would mean maximizing a very messy function over 401 parameters.

If we are interested in testing MVE, but not in actually obtaining the constrained coefficient estimates, we do not need to estimate the constrained set of equations. A Wald test can be performed using only the unrestricted model. In this case, the unconstrained model (6) is particularly easy to estimate, because it requires only equation-by-equation ordinary least squares. Engel and Rodrigues (1988) provide an expression for the Wald statistic for the MVE restrictions. The Wald

<sup>19</sup> In order to save space, we do not report these results.

statistic is not difficult to compute even for large collections of assets. We tested the MVE restrictions for the entire set of 20 industry portfolios composed by Stambaugh, in part to demonstrate the attractiveness of the Wald test version of the CASE method. We again reject the MVE restrictions easily. The test statistic is distributed  $\chi_{19}^2$ , and has a value of 58.99, well above the 99 percent level.<sup>20</sup>

The estimates of this section provide little support for MVE of the stock market. In all of the tests performed, the restrictions that MVE places on a more general asset demand model are strongly rejected.

#### 4. Tests of MVE with ARCH conditional variances.

In the estimates reported in section 3, we assumed that return covariance matrix,  $\Omega_t$ , was constant over time. Because it has become clear in recent years that conditional variances show a considerable amount of variation, we turn to a model of time-varying conditional variances.

In simple regression models, the presence of heteroskedasticity often does not affect the consistency of the coefficient estimates, although it does cause standard calculations of test statistics to be inconsistent. When the MVE restrictions are imposed, however, changes in variances imply changes in coefficient estimates, which in turn imply changes in expected excess returns. The coefficient on the asset shares in the constrained model must move over time if  $\Omega_t$  does, so holding  $\Omega_t$  constant leads to inconsistent coefficient estimates.

Inspection of (2) makes it easy to see why it is important to allow for variation in  $\Omega_t$ . There are two possible sources of variation in expected returns if  $\rho$  is constant: changes in asset shares,  $\lambda_t$ , and changes in  $\Omega_t$ . Suppose, for example, that favorable news about a stock is announced. One could easily think of cases in which the price is pushed up, increasing the stock's share in the aggregate portfolio, even though its expected return is now lower with the news. If the market is mean-variance efficient, this can happen when the riskiness of the asset declines – its own variance falls, or its variance with other assets declines. But, for the jth asset, this is exactly a change in the jth row of  $\Omega_t$ .

The burgeoning econometric literature that proposes general corrections for heteroskedasticity

 $<sup>^{20}</sup>$  The comparable Wald test for the 11-asset aggregation yields a statistic distributed as  $\chi^2_{10}$  equal to 22.76. This also rejects the MVE restrictions at the 99 percent level. These particular tests restrict only the diagonal elements of the return covariance matrix, and yet they reject easily.

is not applicable to this model. That literature relies generally on procedures in which consistent estimates of the residuals are obtained before any heteroskedasticity correction is made, and those estimated residuals are used to construct heteroskedasticity-consistent statistics. In our MVE tests, we must correct for time-varying variances when we estimate the regression coefficients because the coefficients move with the variance. In order to do this, we need an explicit model of the variance process.

We choose to model variances empirically following Engle's (1982) ARCH process. The ARCH takes the conditional variance of this period's forecast error to be a function of past forecast errors. It is not based on any theoretical notion of how the general equilibrium of the economy works. It is an ad hoc model that seems to work well in practice.

The univariate representation of a first-order ARCH would be  $\sigma_{t,i}^2 = \alpha + \gamma \epsilon_{t,i}^2$ . The variance of the forecast error of the *i*th stock between time t and t+1 is given by  $\sigma_{t,i}^2$ , and  $\epsilon_{t,i}^2$  is the square of the forecast error made between time t-1 and t. This equation states that if we make a large forecast error in one period, the variance of our forecast for the next period will be greater (assuming  $\gamma > 0$ ).

In this section, we apply a multi-equation version of ARCH to the MVE problem. Because of the difficulty in estimating large ARCH systems, we have further aggregated the assets into the 7 portfolios described in table 1. Even with only 7 equations to estimate, the dimension of the ARCH problem can be quite large. For example, even if we restrict ourselves to first-order ARCH in which the variances and covariances this period are related only to the squares and cross-products of forecast errors from the previous period, the problem is unmanageably large. There are 28 independent elements in the covariance matrix. If each element were linearly related to the 28 lagged squares and cross products of the forecast errors, there would be 812 variables to estimate. More general forms of ARCH would relate the variance to more than one lag of the cross-products of forecast errors, or to lagged variances (as in Bollerslev's, 1986, GARCH).

Given the complexity of estimating the MVE-ARCH system, and given the limited amount of data, it is helpful to lower the number of ARCH coefficients. Our test of MVE uses a parsimonious version of ARCH, in which the model,

$$E_t(r_{t+1}) = \rho \Omega_t \lambda_t, \tag{8}$$

has return variance given by:

$$\Omega_t = P^t P + G \epsilon_t \epsilon_t^t G.$$

We treat as parameters the upper triangular matrix P, and the diagonal matrix G. Under this formulation, each element of  $\Omega_t$  is linearly related to its corresponding component in the matrix of cross-products of lagged forecast errors. There are only 35 coefficients to estimate. A further advantage of the ARCH in (9) is that it enforces positive semi-definiteness on the covariance matrix  $\Omega_t$ . This turns out to be helpful in estimating the constrained model by maximum likelihood.

The unrestricted form of the inverted system of asset demand equations is given by:

$$E_t(r_{t+1}) = \mathbf{A}_t \lambda_t. \tag{9}$$

MVE imposes the restriction that  $A_t = \rho \Omega_t$ , where  $\Omega_t$  is the conditional variance of  $\tau_{t+1}$ . In practice, if MVE is to be nested in the general system of asset demands, then the elements of  $A_t$  in the general system might be related to the same variables that  $\Omega_t$  is assumed to be related to, but in an arbitrary way. More specifically, we assume that in the unrestricted model, the coefficient matrix  $A_t$  evolves according to:

$$\mathbf{A}_t = Q'Q + F\epsilon_t'\epsilon_t F,\tag{10}$$

where Q is upper triangular and F is diagonal, and the conditional covariance matrix of returns,  $\Omega_t$ , is given by (8). The MVE constraint, that  $\mathbf{A}_t = \rho \Omega_t$ , imposes 34 additional constraints on the unconstrained asset demand equations in (9).

For our restricted ARCH-MVE model in (8), the log-likelihood for observation t is given by:

$$\mathcal{L} = -(7/2)\ln(2\pi) - (1/2)|\Omega_t| - (1/2)(r_{t+1} - \rho\Omega_t\lambda_t)'\Omega_t^{-1}(r_{t+1} - \rho\Omega_t\lambda_t), \tag{11}$$

where  $\Omega_t$  is defined in (8), and  $\epsilon_t = r_t - \rho \Omega_{t-1} \lambda_{t-1}$ . Maximization of (11) is difficult for several reasons. First is the constraint between coefficients and variances. Second is the recursive nature of the problem (so that the likelihood at t, defined above, depends on all observations from 1 to t). Third is the large number of parameters to estimate simultaneously. We estimated the system on a modified version of a maximum likelihood program available in the Gauss programming package. It uses a technique based on the Berndt, Hall, Hall and Hausman (1974) algorithm.

Before turning to the results of the ARCH estimation, it is useful first to examine the constrained MVE estimates on the 7 equation system when  $\Omega_t$  is constrained to be constant, as in the previous section. Table 4 shows that the 7-equation system performs much like its 11-equation counterpart. The estimate of  $\rho$  is close to 2.0. However, it is still not statistically different from zero, which indicates that the asset share data with the MVE constraints imposed do a poor job of explaining expected returns. The log-likelihood with MVE imposed is 5558.56. This compares to a log-likelihood of 5603.56 for the corresponding constant-coefficient, unconstrained system of asset demand equations. In this case, MVE imposes 27 constraints on the general system. The test statistic is distributed  $\chi^2_{27}$ , with a size of 70.00. The MVE constraints can be rejected strongly at the 99 percent level.

Table 5 reports the results of the MVE restrictions imposed on the ARCH system. There are two hypotheses to test here. The first asks whether we can reject the constant-variance MVE model in favor of the ARCH-MVE. A rejection would imply that time-varying variances statistically reduce the distance between the stock-market portfolio and the mean-variance efficient frontier. Such a rejection would lead us to the other interesting hypothesis: can we reject the restrictions implied by MVE on the unrestricted ARCH system in (9) and (10)? This would involve a test of the hypothesis that Q = P and F = G.

The log-likelihood for the ARCH-MVE model in (9) is 5573.97. The constant variance version of MVE is a special case of this ARCH model, in which the G matrix from (9) is constrained to be zero. This imposes 7 constraints on the ARCH system. Our test statistic is 30.82 and is distributed  $\chi_7^2$ : we reject the constant-variance restrictions at the 99 percent level. ARCH therefore improves significantly on the constant-variance form of MVE.

Four of the 7 ARCH coefficients (elements of the G matrix) are significantly different from zero at the 95 percent level. These coefficients are all quite small in magnitude. The square of each element gives the coefficient relating the variance in each equation to its own lagged squared forecast error. Only one of the squared components of G is greater than .10.

The point estimate of  $\rho$  is 1.91 – again close to the Samuelson value of 2.0. Once again, the estimate is not statistically different from zero at the 95 percent level (although it is now significant at the 80 percent level). The most important question is whether the ARCH-MVE model is too

restrictive relative to the general ARCH system given in (9) and (10). This system will produce a log-likelihood value at least as large as the value we reported above - 5603.56 - for the version of the unconstrained model in which  $A_t$  is constant. But even if its likelihood was no larger than this, the size of the test statistic (distributed  $\chi^2_{34}$ ) for testing the MVE constraints on the ARCH model would be 59.18. MVE would therefore be rejected at the 99 percent level. So we do not even need to estimate the unconstrained asset-pricing equations with  $A_t$  varying over time to know that MVE is rejected.

We conclude that while letting the variance change over time is important in improving the explanatory power of MVE, it does not improve it enough relative to an unconstrained system of asset-demand equations.

#### 5. Summary of conclusions

Figure 1 provides a graphical summary of our nested hypothesis tests. At the top of the figure is the most unrestricted model we consider, the unrestricted ARCH model in equations (9) and (10). At the bottom of the figure is the most restrictive model, that asset shares are of no help in explaining required returns, or equivalently, that risk aversion is zero. For each pair of models, the line connecting them reports the results of a test of whether the lower model (the null hypothesis) can be rejected in favor of the upper model (the alternative hypothesis). It is easy to see that both of the MVE formulations – the constant-variance case in equation (7) and the ARCH case in (8) – are rejected when compared with any more general alternative hypothesis. Worse, there is no evidence in favor of these MVE models even when they are pitted as alternative hypotheses against the straw-man model in which asset shares don't matter at all ( $A_t = 0$  in equation (9)).

There are several ways to rationalize these results. One would be that the true asset pricing model is not the CAPM, but rather the APT, a version of the intertemporal CAPM, or even the one-period CAPM plus some other omitted variable. A second explanation for the results would rely on the Roll (1977) critique. If the stock market is very unlike the true "market" portfolio, we would not expect to find MVE, even if the CAPM holds.<sup>21</sup>

Indeed, under this explanation, the asset shares and ARCH processes cannot be accurately observed. A third explanation of the results would be that the residuals in (2) lead to poor measures of the conditional variances. If "peso problems" affect stock market returns, the estimated residuals will be biased. Imposing the MVE restrictions only compounds the problems. For example, it is well known that in the five years following the stock-market boom of August 1982, the market rose at an average annual rate of 22 percent. Few would argue in retrospect that it is possible to obtain from this period ex post, valid measures of ex ante expected risk and return.

One could imagine other reasons as well why the hypothesis of mean-variance efficiency may fail to describe the asset price movements of a given sample. But all the more motivation for developing ever-better tests of the MVE hypothesis a process to which this paper was intended to contribute.

<sup>&</sup>lt;sup>21</sup> Similar results were found, however, when money, bonds, and real estate were allowed into the portfolio (Frankel, 1985a,b, and Frankel and Dickens, 1984) and when foreign assets were allowed (Frankel, 1982, and Frankel and Engel, 1984).

#### 6. References

- Berndt, E., R. Hall, B. Hall, and J. Hausman, "Estimation and Inference in Nonlinear Structural Models," Annals of Economic and Social Measurement, 3 (1974), 653-55.
- Bodurtha, James N., Jr., and Nelson C. Mark, "Testing the CAPM with Time-Varying Risks and Returns," Ohio State University, 1987.
- Bollerslev, Tim, "A Conditionally Heteroskedastic Time Series Model for Security Prices and Rates of Return Data," Northwestern University, 1985.
- Bollerslev, Tim, "Generalized Autoregressive Conditional Heteroskedasticity," Journal of Econometrics, 31 (1986), 307-327.
- Bollerslev, T., R.F. Engle, and J.M. Wooldridge, "A Capital Asset Pricing Model with Time-Varying Covariances," Journal of Political Economy, 96 (1988), 116-131.
- Cox, W.M., "The Behavior of Treasury Securities; Monthly 1942-1984," Research Paper no. 8501, Dallas Federal Reserve Bank of Dallas, 1985.
- Engel, Charles, and Anthony Rodrigues, "A Wald Test of International CAPM," University of Virginia, 1988.
- Engel, Charles, and Anthony Rodrigues, "Tests of International CAPM with Time-Varying Covariances," forthcoming in Journal of Applied Econometrics, 1989.
- Fama, Eugene F., and Kenneth R. French, "Permanent and Temporary Components of Stock Prices," Journal of Political Economy, 96 (1988), 246-273.
- Ferson, K.R., S. Kandel, and R.F. Stambaugh, "Tests of Asset Pricing with Time-Varying Expected Risk Premiums and Market Betas," Journal of Finance, 42 (1987), 201-220.
- Frankel, Jeffrey A., "In Search of the Exchange Risk Premium: A Six-Currency Test of Mean-Variance Efficiency," Journal of International Money and Finance, 2 (1982).
- Frankel, Jeffrey A., "Portfolio Shares as 'Beta-Breakers'," Journal of Portfolio Management, 11 (1985a), 18-23.
- Frankel, Jeffrey A., "Portfolio Crowding-out, Empirically Estimated," Quarterly Journal of Economics, 100 (1985b), 1041-1065.
- Frankel, Jeffrey A., and William Dickens, "Are Asset-Demand Functions Determined by CAPM?," University of California, Berkeley, 1984.
- Frankel, Jeffrey A., and Charles Engel, "Do Asset Demand Functions Optimize Over the Mean and Variance of Real Returns? A Six Currency Test," Journal of International

- Economics, 17, December 1984.
- French, Kenneth R. and Richard Roll, "Stock Return Variances," Journal of Financial Economics, 17 (1986), 5-26.
- Gibbons, Michael R., and Jay Shanken, "Subperiod Aggregation and the Power of Multivariate Tests of Portfolio Efficiency," Journal of Financial Economics, 19 (1987), 389-394.
- Gibbons, M.R., S. Ross, and J. Shanken, "A Test of the Efficiency of a Given Portfolio," Stanford University, 1986.
- Hansen, Lars P., and Scott Richard, "The Role of Conditioning Information in Deducing Testable Restrictions Implied by Dynamic Asset Pricing Models," *Econometrica*, 55 (1987), 587-614.
- Ibbotson Associates, Stocks, Bonds, Bills and Inflation: 1986 Yearbook, (Ibbotson Associates: Chicago) 1986.
- MacKinlay, Craig, "On Multivariate Tests of the CAPM," Journal of Financial Economics, 18 (1987), 341-371.
- Markowitz, H.M., "Portfolio Selection," Journal of Finance, 1952, 77-91.
- Pindyck, R.S., "Risk, Inflation, and the Stock Market," American Economic Review, Vol. 74, pp. 335-51, June 1984.
- Poterba, J.M. and L.H. Summers, "The Persistence of Volatility and Stock Market Fluctuations," American Economic Review, Vol. 76, pp. 1142-1151, 1986.
- Poterba, James M., and Lawrence Summers, "Mean Reversion in Stock Returns: Evidence and Implications," NBER Working Paper no. 1987.
- Rayner, R.K., "Generalized Instrumental Variables Estimation under Rational Expectations on First and Second Moments," Ohio State University, 1986.
- Roll, Richard, "A Critique of the Asset Pricing Theory's Tests; Part I: On Past and Potential Testability of the Theory," Journal of Financial Economics, 4 (1977), 129-76.
- Schwert, G. William, "Size and Stock Returns, and other Empirical Regularities," Journal of Financial Economics, 12 (1983), 3-12.
- Shanken, Jay, "Multivariate Tests of the Zero Beta CAPM," Journal of Financial Economics, 14 (1985), 327-48.
- Stambaugh, R., "On the Exclusion of Assets from Tests of the Two Parameter Model: A Sensitivity Analysis," Journal of Financial Economics, 10 (1982), 237-268.

- Tobin, James, "Liquidity Preference as Behavior toward Risk," Review of Economic Studies, 67, (February 1958) 8-28.
- Tobin, James, "The General Equilibrium Approach to Portfolio Balance Theory," Journal of Money, Credit and Banking, 1 (1969).
- Tobin, James, "Liquidity Preference, Separation, and Asset Pricing," Zeitschrift für betriebswirtschaft, 53 (March 1983), 236-38.
- Wills, H., "Inferring Expectations," London School of Economics, 1982.

<u>Table 1</u>
Industry Portfolios and S.E.C. Codes

# 11 Portfolios (Combinations of the 20 portfolios)

Portfolio	<u>Industry Portfolios</u>
1	1, 20
2	2, 3, 4
3	5
4	6
5	7, 8, 9
6	10
. 7	11
8	12-15
9	16
10	17, 18
11	19

# 7 Portfolios (Combinations of the 20 portfolios)

<u>Portfolio</u>	<u>Industry Portfolios</u>
1	1, 2, 3, 4, 20
2	5, 7, 8, 9
3	6
4	10, 11
5	12-15
6	16
ī	17-19

Table 2

## Estimated Coefficients from Unconstrained OLS Regressions

Dependent Variable: Excess rate of return on asset j Independent Variables: Shares of asset j in total portfolio

	•									
1	12	<del>1</del> 3	<u>λ<sup>4</sup></u>	<u>\lambda^5</u>	<del>1</del> 6	<del>\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ </del>	<u>λ</u> 8	<del>1</del> 9	$\frac{\lambda^{10}}{}$	111
Equation	<u>on 1</u>	•								
									-0.35 (0.25)	
		(0.00)								(0.44)
R	023		Brei	usch-Goo	ifrey st	tatistic	: (20 la	ags) = 4	12.79	
<u>Equation</u>										
									0.83	
(0.13)	(0.86)	(0.32)	(0.27)	(0.34)	(0.26)	(0.46)	(0.23)	(0.22)	(0.57)	(1.24)
$R^2$	050		Bre	usch-Goo	ifrey s	tatistic	(20 la	ags) = :	23.38	
Equation	<u>on 3</u>									
-0.20	-1.05	0.12	-0.04	-0.32	0.14	-1.20*	-0.02	0.46*	1.16	2.05
(0.13)	(0.89)	(0.33)	(0.28)	(0.35)	(0.27)	(0.47)	(0.24)	(0.23)	(0.59)	(1.29)
$R^2$	= .047	Breusch-Godfrey statistic (20 lags) = 16.99								
Equati	on <u>4</u>									
0.15	-0.55	0.74	-0.82*	-0.81*	0.14	-1.01	0.44	-0.01	-0.60	2.79
									(0.72)	
$R^2$	= .027		Bre	usch-Go	dfrey s	tatistic	20 1	ags) =	21.74	
Equati	<u>on</u> 5									
									-0.02	
(0.16)	(1.07)	(0.39)	(0.34)	(0.42)	(0.33)	(0.57)	(0.29)	(0.28)	(0.71)	(1.55)
$R^2$	= .044		Bre	usch-Go	dfrey s	tatisti	c (20 1:	ags) =	30.71	
Equati	on 6									
	<u> </u>									
		0.46	-0.40	-0.68	-0.45	-0.28	0.37	0.18	-0.06	1.99
-0.10	-0.19								-0.06 (0.69)	

Table 2 (continued)

	12	<del>- 1 3</del>	14	15	16	77	<u>, 8</u>	9	110	111
<u>Equation</u>	<u>7</u>	٠								
-0.17 -2 (0.17) (1	.72 <sup>*</sup> .13)	0.83*	-0.26 (0.36)	0.71 (0.44)	0.44	-2.15 <sup>*</sup> (0.60)	0.37 (0.30)	0.75 <sup>*</sup> (0.29)	1.21 (0.75)	3.15 (1.63)
$R^2 = .0$	066		Bre	usch-Go	ifrey s	tatistic	= (20 la	ags) = [	17.38	
Equation 8										
-0.14 -0. (0.14) (0.	.85 .93}	0.25 (0.34)	-0.10 (0.29)	-0.43 (0.36)	0.08 (0.29)	-1.41 <sup>*</sup> (0.49)	-0.04 (0.25)	0.62	0.94 (0.62)	1.80 (1.34)
$R^2 = .0$	067		Bre	usch-God	ifrey s	tatistic	e (20 ls	ags) = 1	21.10	
Equation 9	2				·		,		••••	
-0.09 -0. $(0.12) (0.$	.77 .80)	0.50 (0.30)	-0.10 (0.25)	-0.12 (0.31)	0.18 (0.25)	-0.64 (0.43)	-0.04 (0.21)	0.30	0.07	0.82
$R^2 = .0$		(0.30) (0.25) (0.31) (0.25) (0.43) (0.21) (0.21) (0.53) (1.16)  Breusch-Godfrey statistic (20 lags) = 35.07*								
Equation 1	10									
-0.11 -0. (0.16) (1.	.38 .06)	0.20 (0.39)	-0.10 (0.33)	-0.27 (0.42)	0.01 (0.33)	-0.56 (0.56)	0.06 (0.28)	0.41 (0.28)	-0.02 (0.70)	1.05 (1.53)
$R^2 = .0$	27	Breusch-Godfrey statistic (20 lags) = 44.68*								
Equation 1					·			- <b>L</b>		
-0.04 -0. (0.14) (0.	25 95)	0.13 (0.35)	0.19	0.09 (0.37)	0.24 (0.29)	0.13 (0.50)	0.19 (0.25)	0.54 (0.25)	-0.20 (0.63)	-1.31 (1.37)
$R^2 = .0$	27		Breu	sch-God	lfrey st	atistic	(20 la	ugs) = 4	2.42*	

<sup>\* =</sup> significant at 95% level

#### Table 3

## CAPM Estimation, constant $\Omega$ , 11 assets

$$r_{t+1} = \rho(P'P)^{\dagger}_{t} + \varepsilon_{t+1}$$

$$Var_t(\varepsilon_{t+1}) = P'P$$

\*\*\* Log Likelihood = -8593.684711 \*:

The estimate of the coefficient  $\rho$ :

2.0319 (1.6130)

The estimate of the upper triangular matrix P:

```
.0398 .0322 .0334 .0385 .0411 .0346 .0404 .0331 .0257 .0316 .0374
(.0018)(.0021)(.0023)(.0028)(.0026)(.0026)(.0030)(.0025)(.0022)(.0029)(.0023)
       .0274 .0197 -.0033 .0166 .0198 .0223 .0189 .0089 .0252 .0047
      (.0011)(.0015)(.0023)(.0019)(.0025)(.0022)(.0019)(.0017)(.0025)(.0015)
              .0204 .0042 .0044 .0097 .0097 .0078 -.0046 .0015 .0000
             (.0008)(.0024)(.0015)(.0019)(.0019)(.0014)(.0018)(.0018)(.0018)
                     .0360 -.0029 -.0019 -.0032 -.0017 .0018 -.0073 .0125
                    (.0014)(.0016)(.0021)(.0019)(.0015)(.0018)(.0019)(.0016)
                            .0276 .0058 .0102 .0090 -.0046 .0003 .0051
                           (.0011)(.0019)(.0019)(.0013)(.0017)(.0017)(.0016)
                                   .0304 .0068 .0050 -.0025 .0021 -.0009
                                 (.0011)(.0016)(.0015)(.0017)(.0018)(.0014)
                                         .0272 .0063 .0000 .0063 .0020
                                        (.0011)(.0014)(.0017)(.0019)(.0017)
                                                .0214 .0020 .0094 .0027
                                               (.0010)(.0018)(.0018)(.0017)
                                                       .0272 .0032 .0050
                                                      (.0011)(.0017)(.0014)
                                                              .0287 .0006
                                                             (.0013)(.0013)
                                                                    .0219
                                                                    (.0007)
```

Table 4

CAPM Estimation, Constant 0, 7 assets

$$\mathbf{r}_{\mathsf{t+1}} = \rho(P'P)^{\lambda}_{\mathsf{t}} + \varepsilon_{\mathsf{t+1}}$$

$$Var_t(\varepsilon_{t+1}) = P'P$$

\*\*\* Log Likelihood = -5558.561247 \*

The estimate of the coefficient  $\rho$ :

2.02778 (1.46639)

The estimate of the upper triangular matrix P:

```
.03842
          .03935
                  .03711
                            .04015
                                     .03640
                                              .02695
                                                       .03782
(.00150) (.00185) (.00246) (.00213) (.00206) (.00190) (.00197)
          .02075 -.00471
                           .01708
                                     .01571 -.00389
                                                       .00485
         (.00075) (.00225) (.00140) (.00149) (.00153) (.00123)
                  .03757 -.00296 -.00242 -.00033
                  (.00115) (.00143) (.00120) (.00166) (.00117)
                            .02435 .00762 -.00136
                           (.00092) (.00137) (.00156) (.00117)
                                     .02206
                                              .00269
                                                       .00735
                                    (.00087) (.00149) (.00108)
                                              .02801
                                                      .00408
                                             (.00103) (.00109)
                                                       .02034
                                                      (.00075)
```

CAPM Estimation, ARCH, 7 assets

$$\mathbf{r}_{\mathsf{t+1}} = \rho \Omega_{\mathsf{t}} \lambda_{\mathsf{t}} + \varepsilon_{\mathsf{t+1}}$$

$$\operatorname{Var}_{\mathbf{t}}(\varepsilon_{\mathbf{t}+1}) = \Omega_{\mathbf{t}} = \operatorname{P'P} + \operatorname{G}\varepsilon_{\mathbf{t}}\varepsilon_{\mathbf{t}}G$$

\*\*\* Log Likelihood = -5573.969787 \*\*\*

The estimate of the coefficient  $\rho$ :

1.91212 (1.47685)

The estimate of the upper triangular matrix P:

.01971

The estimates of the diagonal elements of G:

# Tests of the model

 $r_{i+1} = A_i \lambda_i + \varepsilon_{i+1}$ ;  $E_i \mid \varepsilon_{i+1} \varepsilon_{i+1} \mid = 0_{i+1}$ 

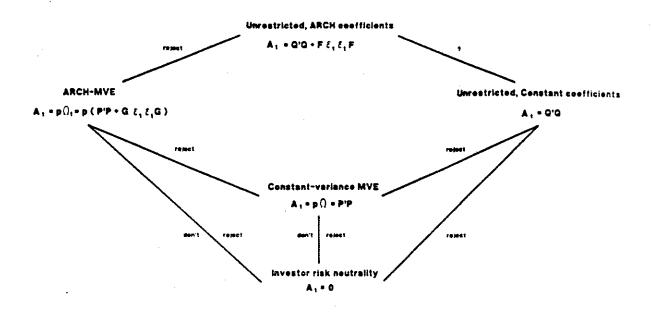


Figure 1

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