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Seo, S Lu, Xin Zhu, J-X <u>et al.</u>

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Disorder in quantum critical superconductors

S. Seo^{1†}, Xin Lu^{2,3†}, J-X. Zhu², R. R. Urbano^{2,4}, N. Curro⁵, E. D. Bauer², V. A. Sidorov^{2,6}, L. D. Pham⁷, Tuson Park^{1*}, Z. Fisk⁷ and J. D. Thompson^{2*}

In four classes of materials—the lavered copper oxides, organics, iron pnictides and heavy-fermion compounds-an unconventional superconducting state emerges as a magnetic transition is tuned towards absolute zero temperature, that is, towards a magnetic quantum critical point¹ (OCP). In most materials, the QCP is accessed by chemical substitution or applied pressure. CeCoIn₅ is one of the few materials that are 'born' as a quantum critical superconductor²⁻⁴ and, therefore, offers the opportunity to explore the consequences of chemical disorder. Cadmium-doped crystals of CeCoIn₅ are a particularly interesting case where Cd substitution induces long-range magnetic order⁵, as in Zn-doped copper oxides^{6,7}. Applied pressure globally suppresses the Cd-induced magnetic order and restores bulk superconductivity. Here we show, however, that local magnetic correlations, whose spatial extent decreases with applied pressure, persist at the extrapolated QCP. The residual droplets of impurity-induced magnetic moments prevent the reappearance of conventional signatures of quantum criticality, but induce a heterogeneous electronic state. These discoveries show that spin droplets can be a source of electronic heterogeneity and emphasize the need for caution when interpreting the effects of tuning a correlated system by chemical substitution.

Impurities, defects in an otherwise homogeneous host, often are unwanted because their influence can mask intrinsic properties of the host material⁸. Impurities, however, also can be a double-edged sword by providing an avenue to induce interesting new phases of matter and to probe the underlying mechanism of exotic ground states, especially those that emerge from complex interactions in strongly correlated electron materials. In the high-transitiontemperature (T_c) copper oxide superconductors, the intentional inclusion of small concentrations of non-magnetic impurities, such as Zn, induces magnetism around the impurity site and also enables visualization of the symmetry of the superconducting gap^{6,7,9,10}. Nucleation of a charge density wave in regions surrounding impurity sites is another example of defects revealing the underlying competing phase by disorder¹¹. With a growing number of classes of materials that show unusual sensitivity to impurities, understanding and controlling the emergent phases from impurities is an important open issue.

Materials that exhibit an extreme sensitivity to impurities often are near a zero-temperature, second-order phase transition, where quantum critical fluctuations of the associated order parameter diverge in space and time. Theory predicts that when disorder is coupled to these critical fluctuations local regions of an exotic phase can nucleate inside the host and change the nature of the phase transition; indeed, even long-range order of the nucleated phase is possible¹²⁻¹⁴. Nuclear magnetic resonance and scanning tunnelling microscopy have validated these predictions by showing that the host system locally responds to an impurity by creating an extended droplet of the new phase around an impurity^{6,15}. Understanding how the local droplet evolves as a function of a control parameter or how the droplet interplays with the host phase, however, is less well known, partly owing to a lack of very pure compounds that are situated sufficiently close to a QCP. The quantum critical superconductor CeCoIn₅ provides an ideal opportunity to probe the consequences of impurities on fluctuations of a quantum critical state. It forms readily as exceptionally high-quality single crystals, and the small ($\sim 1 \text{ meV}$) characteristic energy of its ground state can be tuned easily with modest applied pressure or magnetic field without introducing additional disorder¹⁶⁻¹⁸. At ambient pressure, the quantum critical state of CeCoIn₅, characterized by a linear-in-temperature electrical resistivity above T_c (ref. 3) and logarithmic divergence of the low-temperature electronic specific heat divided by temperature (C/T) (ref. 19), has been interpreted as being due to proximity to a field-induced magnetic QCP (refs 16,20). Replacing one atomic per cent of In by Cd in CeCo $(In_{1-x}Cd_x)_5$ reduces T_c from 2.3 K (x = 0) to $T_c = 1.2 \text{ K} (x = 0.01)$ and induces microscopic coexistence of long-range antiferromagnetic order with $T_{\rm N} = 2.8 \,\mathrm{K}$ (refs 5,21). For slightly larger x, superconductivity is suppressed completely and only Néel order remains. Introducing these Cd atoms into CeCoIn₅ creates defects that produce a response consistent with theoretical expectations¹²⁻¹⁴.

Application of pressure accurately reverses the global effect of Cd substitutions, suppressing the long-range magnetic order and inducing a dome of superconductivity⁵. The fact that the global phase response of CeCoIn₅ to cadmium doping can be undone by applied pressure suggests that a quantum critical state should reappear, but the critical point may be hidden by the pressure-induced superconducting state of Cd-doped crystals. This is precisely what is found in the isostructural compound CeRhIn₅, which orders antiferromagnetically at atmospheric pressure in the absence of intentionally added impurities. Applying pressure to this correlated electron metal suppresses its long-range antiferromagnetism and induces a dome of bulk superconductivity that hides a QCP that is revealed in an applied magnetic field^{17,18}. The pressure evolution of C/T in zero-field is shown in Fig. 1a as a function of temperature for CeCoIn5 doped with 1% Cd. Similar results are found for a sample doped with 1.5% Cd (see Supplementary Fig. 1). For comparison, we also plot the pressure dependence of C/T of the pristine reference compound CeRhIn₅ in Fig. 1b. With applied

¹Department of Physics, Sungkyunkwan University, Suwon 440-746, South Korea, ²Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA, ³Center for Correlated Matter and Department of Physics, Zhejiang University, Hangzhou 310027, China, ⁴Instituto de Fisica 'Gleb Wataghin', Universidade Estadual de Campinas-SP, 13083-859, Brazil, ⁵Department of Physics, University of California, Davis, California 95616, USA, ⁶Institute for High Pressure Physics, Russian Academy of Sciences, RU-142190 Troitsk, Moscow, Russia, ⁷Department of Physics, University of California, Irvine, California 92697, USA. [†]These authors contributed equally to this work. *e-mail: tp8701@skku.edu; jdt@lanl.gov



Figure 1 | **Pressure dependence of the specific heat of 1% Cd-doped CeColn₅ and CeRhIn₅. a**, Specific heat divided by temperature for 1% Cd-doped CeColn₅ in zero applied field and at pressures of 0.25 (black symbols), 0.60 (red), 0.98 (blue) and 1.21 GPa (orange). **b**, Specific heat divided by temperature for CeRhIn₅ at 1.15 (black), 1.51 (red), 1.71 (blue) and 2.05 GPa (orange). In CeRhIn₅, the spin entropy of Ce 4*f* local moments is transferred completely to the superconducting phase when magnetism is suppressed, resulting in a large $\Delta C/C_N > 4$ at T_c (ref. 18). The qualitative difference between CeRhIn₅ and Cd-doped CeCoIn₅ exists even though the ordered magnetic moment in both is comparable, ~0.7 µ_B. **c-f**, Dependence on temperature of the specific heat divided by temperature of 1% Cd-doped CeCoIn₅ under magnetic fields and pressures. **c**, 0.25 GPa at magnetic fields of 0 (black), 1.0 (red), 3.0 (green), 5.0 (blue) and 9.0 T (orange). **d**, 0.6 GPa at magnetic fields of 0 (black), 1.0 (red), 3.0 (blue) and 5.0 T (orange). **e**, 0.98 GPa at magnetic fields of 0 (black), 2.0 (red), 4.0 (green), 5.0 (blue) and 5.5 T (orange). **f**, 1.54 GPa at magnetic fields of 0 (black), 3.0 (red), 4.0 (green), 5.0 (blue) and 6.0 T (orange). Solid and dashed arrows indicate superconducting and antiferromagnetic transition temperatures, respectively. Values of *C/T* for different pressures were normalized against each other with an assumption that the entropy recovered at 10 K is the same for all pressures within each compound. This assumption is proved for Cd-doped CeColn₅ as a function of Cd content at atmospheric pressure⁵.

pressure, T_N is suppressed in both CeRhIn₅ and Cd-doped CeCoIn₅ compounds, and T_c increases. In contrast to CeRhIn₅, however, the discontinuity $\Delta C = C - C_N$, where C_N is the normal-state specific heat at T_c , normalized by C_N , $\Delta C/C_N \approx 1.2$ at T_c for Cd-doped CeCoIn₅ at P = 1.21 GPa. This normalized discontinuity is less than 30% of the corresponding value in CeRhIn₅ at 2.05 GPa or in pure CeCoIn₅ at ambient pressure where these materials have nearly identical T_c values.

The effect of a magnetic field on the specific heat of the 1% Cd-doped CeCoIn₅ is summarized in Fig. 1c–f for pressures up to 1.54 GPa. For magnetic fields above the critical field B_{c2} ,

where superconductivity is completely destroyed, C/T at low temperatures decreases with decreasing temperature typical of a non-critical metal. At 0.98 GPa and 6.2 T, which is just above the upper critical field B_{c2} at this pressure, there is a slight upturn in C/T at the lowest temperatures. This weak upturn, however, is distinct from undoped CeCoIn₅, where C/T logarithmically diverges with decreasing temperature near B_{c2} (ref. 16) and from CeRhIn₅ at its quantum critical pressure, where C/T also diverges once superconductivity is suppressed by a magnetic field¹⁸. The prominent lack of a divergence in C/T of the Cd-doped compound indicates that quantum critical behaviour is avoided.

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Figure 2 | **Electrical resistivity of 1% Cd-doped CeCoIn5** under pressure. **a**, Contour map of the electrical resistivity (ρ_{ab}) within the Ce-In plane plotted in the pressure-temperature plane. T_{max} is a temperature where the resistivity reaches a maximum, and T^* is the temperature below which the resistivity deviates from a *T*-linear dependence. An antiferromagnetic state coexists with superconductivity for P < 0.5 GPa. **b**, In-plane resistivity ρ_{ab} as a function of temperature on a semi-logarithmic scale for representative pressures. Arrows mark the evolution of T_{max} with pressure. The temperature T_{max} at which $\rho(T)$ is a maximum occurs at 34 K at ambient pressure and increases linearly with increasing pressure, which is typical of strongly correlated Ce-based materials, such as pure CeCoIn₅, and reflects a pressure-induced increase of the hybridization between ligand electrons and the periodic array of Ce 4*f*-electrons. **c**, Resistivity, with the residual T = 0 value subtracted, divided by temperature, plotted against temperature for representative pressures. T^* is marked by arrows.

Supporting this lack of quantum criticality from specific heat measurements, the electrical resistivity ρ of 1% Cd-doped CeCoIn₅ also does not show an anomalous temperature dependence characteristic of proximity to a QCP. Isothermal cuts of the low-temperature electrical resistivity as a function of pressure (Fig. 2a) show that $\rho(P)$ decreases monotonically for $T \ge T_c$ across the critical pressure $P_{c1}(= 0.5 \text{ GPa})$, where T_N becomes equal to T_c , and $P_{c2}(= 1.0 \text{ GPa})$, the extrapolated critical point where T_N extrapolates to 0K inside the superconducting dome. Further, Fig. 2c shows a linear-*T* resistivity over a temperature range between 12 and 35 K at 1.89 GPa, but it becomes sub-linear in *T* at lower temperatures, in contrast to expectations of quantum

criticality and the *T*-linear $\rho(T)$ in pristine CeCoIn₅ that extends to T_c (ref. 3). This sub-linear temperature dependence of the resistivity demonstrates that the spectrum of spin excitations has changed with doping such that the scattering rate below T^* is reduced relative to a continuation of the *T*-linear resistivity to lower temperatures, a reduction in scattering arising from possible short-range magnetic correlations.

The large jump in specific heat at T_c in pure CeCoIn₅ and in CeRhIn₅ at its pressure-tuned QCP is a consequence of the huge quantum disordered entropy of magnetic fluctuations that is recovered in the zero-temperature limit when superconductivity is suppressed by a magnetic field. In contrast, the specific

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heat jump in Cd-doped CeCoIn₅ is smaller, even when these crystals are tuned to their putative critical point. This small jump, together with the absence of a signature for a diverging specific heat in a magnetic field and *T*-linear $\rho(T)$ to T_c , indicates that the spectrum of magnetic fluctuations has changed in response to the presence of Cd impurities. When very dilute concentrations of non-magnetic impurities are added to CeCoIn₅, a resonance in the electronic density of states develops from unitary scattering of the highly correlated band of conduction electrons by the local defect²². In this process, the non-magnetic defect acquires the magnetic character of a spin S = 1/2 Kondo impurity. At higher concentrations, local droplets of static magnetic order nucleate with a typical extent of a few lattice parameters²¹, and when these droplets overlap, long-range antiferromagnetic order develops.

magnetic fluctuations may be suppressed locally through the nucleation of spin droplets around the Cd impurities, they should not be affected significantly at distances removed from these impurities where there is no static magnetism. Apparently, sufficient spectral weight remains in the unaffected fluctuations to produce a superconducting transition only slightly lower than that of pure CeCoIn₅.

Figure 3a shows ¹¹⁵In nuclear quadrupolar resonance (NQR) spectra of the In(1) site for CeCoIn₅ and 1% Cd-doped CeCoIn₅. Three peaks A, B and C are observed in Cd-doped crystals²¹, where peak A probes the bulk of the unit cells as in pristine CeCoIn₅. The existence of B and C peaks underscores the presence of a minority of In sites in an electronic environment not present in undoped CeCoIn₅. Cd impurities significantly broaden the In(1) NQR spectra owing to the distribution of

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local electric field gradients. Figure 3b shows the temperature dependence of the spin-lattice relaxation rate $1/T_1$ measured at peak A of 1% Cd-doped CeCoIn₅ under pressures to 1.51 GPa. At ambient pressure, $1/T_1$ is identical to the pure compound and follows a $T^{1/4}$ temperature dependence in the disordered state, which is expected for a system in close proximity to an antiferromagnetic QCP (refs 21,23). The observation that $1/T_1$ is a strong function of pressure yet independent of Cd doping provides microscopic evidence that pressure is not the reverse of doping. Taken with the specific heat data, these data imply that the electronic response to Cd doping is strongly inhomogeneous. As pressure tunes the system away from longrange magnetic order, the spin-spin correlation length, ξ , and therefore the size of the droplets, should decrease. In the temperature range around T_N (P = 0), this is reflected in a rapid decrease of the relaxation rate $1/T_1 \propto T\xi^{\alpha}$ (refs 23–27) that is plotted in Fig. 3b. These NQR results provide microscopic 2 evidence for the existence of spin droplets even when global

pressures above P_{c1} . The nucleation and pressure evolution of spin droplets can be understood within the framework of a theoretical model that considers the competition between antiferromagnetism and d-wave superconductivity¹³ (details of the model are discussed in Supplementary Information). In the absence of impurities, this model gives negligible spectral weight in the magnetic channel and homogeneous *d*-wave superconductivity near a OCP. When a unitary scattering impurity is introduced, however, superconductivity is suppressed strongly around the defect but recovers over a distance of a coherence length away from the impurity. Concurrently, magnetic order is depressed at the impurity but is a maximum at the nearest Ce neighbour and decays over many lattice constants. As shown in Supplementary Fig. 4a,b, the superconducting order is robust against a change in effective bandwidth (or the external pressure), but the magnetic order is very sensitive. A slight increase in bandwidth rapidly dampens the longrange oscillatory magnetization and the amplitude of the nearestneighbour magnetic order parameter. For a dilute concentration of impurity centres or at sufficiently wider bandwidths (higher pressures), there will be only magnetic droplets, but for a narrower bandwidth or higher concentration of scattering centres, magnetic correlations between sites induce global magnetic order. Predictions of this model are illustrated schematically in Fig. 3c.

long-range antiferromagnetic order is suppressed completely for

The lack of signatures for quantum critical behaviour in Cddoped CeCoIn₅ manifests a new mechanism for the coexistence of magnetism and superconductivity and provides a different perspective for interpreting the response to disorder in other strongly correlated superconductors near a zero-temperature magnetic instability. As this work shows, tuning a system with or by disorder to a presumed magnetic QCP does not necessitate a quantum critical response and associated spectrum of quantum fluctuations. Although not all impurities may be unitary scatterers, the likelihood is high that they will be strong scatterers if the bandwidth of the host material is sufficiently narrow, as it is in many strongly correlated heavy-fermion compounds, such as CeCoIn₅. The freezing of magnetic quantum fluctuations around impurity sites has broader consequences for the nature of electronic heterogeneity that is common to classes of strongly correlated electron systems.

Methods

Single crystals of $CeCo(In_{1-x}Cd_x)_5$ were synthesized by a standard In-flux technique and their basic physical properties were reported previously⁵. Electrical resistivity, specific heat and NQR measurements were performed under pressure for samples with Cd concentrations x = 0.01 and 0.015, where the concentration x is determined by microprobe measurements. A quasi-hydrostatic pressure environment was achieved in a Be–Cu/NiCrAl hybrid clamp-type cell with silicone

oil as the transmitting medium and pressure in the cell was determined at low temperatures by inductive measurements of a change in the superconducting transition temperature of Sn that was placed inside the cell²⁸. Specific heat measurements were performed by an a.c. calorimetric technique, where the voltage in Au/Fe(0.07%) thermocouple wire, attached to one facet of the crystal, was monitored and converted to a temperature change that is inversely proportional to the specific heat. Details of the a.c. calorimetric technique can be found elsewhere²⁹. A standard four-probe technique was employed to measure the electrical resistivity using an LR700 resistance bridge. The spin-lattice relaxation time $1/T_1$ at the A site, which is associated with the bulk high-symmetry In(1) sites, was obtained at zero field by measuring the NQR of a single-crystalline sample.

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Author contributions

All authors discussed the results and commented on the manuscript. S.S. and X.L. performed the measurements and contributed equally to this work. R.R.U., V.A.S. and N.C. performed and analysed NQR experiments. E.D.B., L.D.P. and Z.F. provided samples, J-X.Z. performed theoretical calculations and T.P. and J.D.T. wrote the manuscript with input from all authors.

Additional information

Supplementary information is available in the online version of the paper. Reprints and permissions information is available online at www.nature.com/reprints. Correspondence and requests for materials should be addressed to T.P. or J.D.T.

Competing financial interests

The authors declare no competing financial interests.

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